

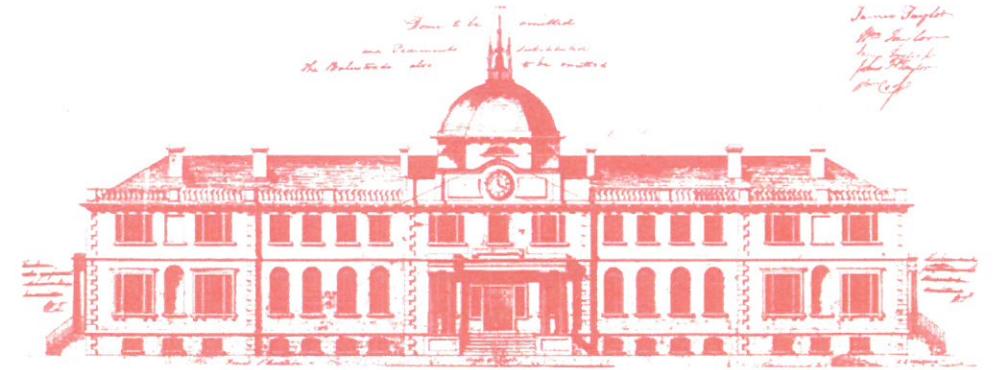
# Line Simplification Under Spatial Constraints

## Abstract

A linear feature is a chain of discrete positions or an abstraction of an areal feature (e.g., road centreline, river) or the outline of a boundary (e.g., coastline, administrative boundary). Spatiotemporal positions of a moving object - a person (with a cellphone, hand held GPS), tagged animal (e.g., study of movement and migratory patterns), moving vehicle (e.g., vessel, car, or plane with GPS navigation), robot (e.g., self-driving car or drone) can be represented as an ordered series of discrete positions (trajectory). A polyline  $L$  defined by  $n$  line segments is an ordered connected chain of  $n + 1$  positions (coordinates).  $L$  can be simple (with no self-crossings) or complex - with planar or non-planar intersections with itself or other polylines to be simplified. The spatial characteristics of  $L$  can also be constrained by other objects (point, lines, or polygons) in an embedding planar space.

Given a polyline  $L$  with  $n$  segments, the line simplification problem seeks to approximate  $L$  as  $L'$  with  $m$  vertices, where  $m < n + 1$ . The goal is to find vertices of  $L$  that represent  $L'$  'well'. In computational graphics, data storage, network transmission, and spatial analysis, it is very beneficial to replace complex geometric objects with simpler ones that capture the relevant features of the original. Out of context simplification of  $L$  can lead to topological errors. In this dissertation, given  $\epsilon > 0$  ( $\epsilon$  - error of approximating  $L$  as  $L'$ ), we restrict the vertices of  $L'$  to be a subset of  $L$  with the following optional constraints: (i)  $L'$  should preserve planar self-intersection and avoid introducing new self-intersections with itself or other polylines, (ii) consecutive segment of  $L'$  should not invert the topological relation in  $L$ , (iii)  $L'$  should preserve disjoint, intersect, minimum distance relation with other planar objects, and (iv)  $L'$  should be homotopic to  $L$  in the context of other planar objects.

Simplification of a polyline or group of polylines with these constraints makes finding a polynomial solution hard [Guibas et al. 1993; Estkowski, 1998; Estkowski and Mitchell, 2001]. The outcomes of this research are development of novel geometric heuristics for simplification of arbitrary static and spatiotemporal polylines in the context of other planar objects. Experimental evaluation showed a competitive compression ratio in a reasonable processing time compared to unconstrained simplification. We also develop geometric tools to make practical our algorithms in industry and data processing.



Home of the School of Graduate Studies, Sir Howard Douglas Hall was designed by J.E. Woolford in 1825 and is the oldest university building in Canada still in use.

## UNIVERSITY OF NEW BRUNSWICK SCHOOL OF GRADUATE STUDIES

ORAL EXAMINATION

**Titus Tienaah**

IN PARTIAL FULFILMENT  
OF THE REQUIREMENTS FOR THE DEGREE OF

DOCTOR OF PHILOSOPHY

Ph.D. Candidate

**Titus Tienaah**

Graduate Academic Unit

**Geodesy & Geomatics Engineering**

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**June 11, 2018**

**2:00 p.m.**

**Head Hall  
Room E-11**

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**Examining Board:**

Dr. Emmanuel Stefanakis (Geodesy & Geomatics Eng.)  
Dr. David Coleman (Geodesy & Geomatics Eng.)  
Dr. Monica Wachowicz (Geodesy & Geomatics Eng.)  
Dr. Susan Nichols (Geodesy & Geomatics Eng.)  
Dr. Suprio Ray (Computer Science)

Co-Supervisor  
Co-Supervisor

**External Examiner:**

Dr. Éric Guilbert  
Département des sciences géomatiques  
Université Laval

**The Oral Examination will be chaired by:**

Dr. John Kershaw, Associate Dean of Graduate Studies

**BIOGRAPHY**

**Universities attended (with dates & degrees obtained):**

2011-2018      **PhD** Candidate, University of New Brunswick  
2008-2011      **MScE**, GGE, University of New Brunswick, Fredericton, Canada.  
2003-2007      **BSc**, Geomatics Engineering, Kwame Nkrumah University of Science and Technology

**Publications:**

**Tienaah, T.**, Stefanakis, E., & Coleman, D.(2018). Line Simplification While Keeping it Simple or Complex ... *In Review*

**Tienaah, T.**, Stefanakis, E., & Coleman, D.(2018). Topologically Consistent Online Trajectory Simplification ... *In Review*

**Tienaah, T.**, Stefanakis, E., & Coleman, D.(2015). Contextual Douglas-Peucker Simplification, *Geomatica* 69(3)327-338.

**Conference Presentations & Proceedings:**

**Tienaah, T.**, Stefanakis, E., & Coleman, D. (2015). Contextual Line Generalization- Extending ArcGIS Generalization Toolset. In Proceedings of the 18th AGILE international conference on geographical information science (pp. 9-12).

**Tienaah, T.**, and Stefanakis, E., (2014). Troy is ours - How on earth could Clytaemnestra know so fast?. In the Proceedings of the 17th AGILE Conference on Geographic Information Science, Castellon, Spain.

**Tienaah, T.**(2014). Real-time Linear Simplification under Space Constraints. In Proceedings of Spatial Knowledge and Information, Banff, Canada.

Sutherland, M. & **Tienaah, T.** & Seeram, A. & Ramlal, B. & Nichols, S.(2013). Chapter 7: Public Participatory GIS, Spatial Data Infrastructure, and Citizen-Inclusive Collaborative Governance. Global Spatial Data Infrastructure Association Press, pp. 123-140.

**Research Projects:**

**Tienaah, T.**, and Stefanakis, E., (2015-2017). Constrained Line Simplification(CLS) for ArcGIS. Engage Project, Industrial partner: Esri Canada.

**Tienaah, T.**, Rak, A. and Coleman, D. (2013). An Examination and Critical Comparison of Alternative Maintenance Models for the Nova Scotia Digital Topographic Database. Contract Report of 2-year consulting study undertaken for the GeoNova Program Office, Service Nova Scotia and Municipal Relations, Province of Nova Scotia. March.

Mioc, D., Anton, F., Nickerson, B., Santos, M., Adda, P., **Tienaah, T.**, et.al. (2011). Flood progression modelling and impact analysis. In Efficient Decision Support Systems- Practice and Challenges in Multidisciplinary Domains. InTech.